



# Towards More Efficient and More Optimal Airport Ground Movement Using Artificial Intelligence

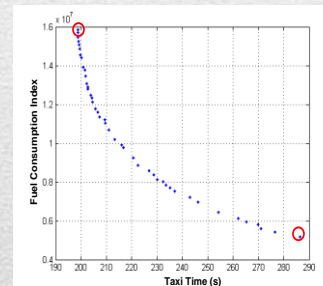
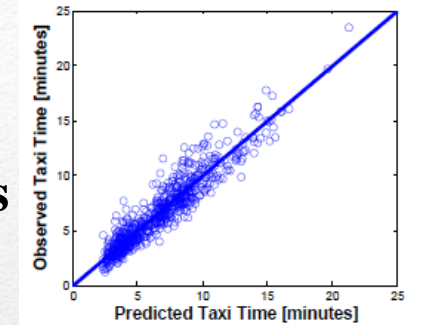
*Dr. Jun Chen*

*Professor Paul Stewart*

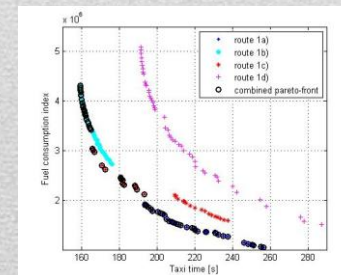


## Outline

- Airside airport operations
- Taxi time estimation using Fuzzy Rule-based Systems
- Trade-off between time and fuel using multi-objective optimisation



- Combined Trade-off and Routing and scheduling algorithm
- Future Work

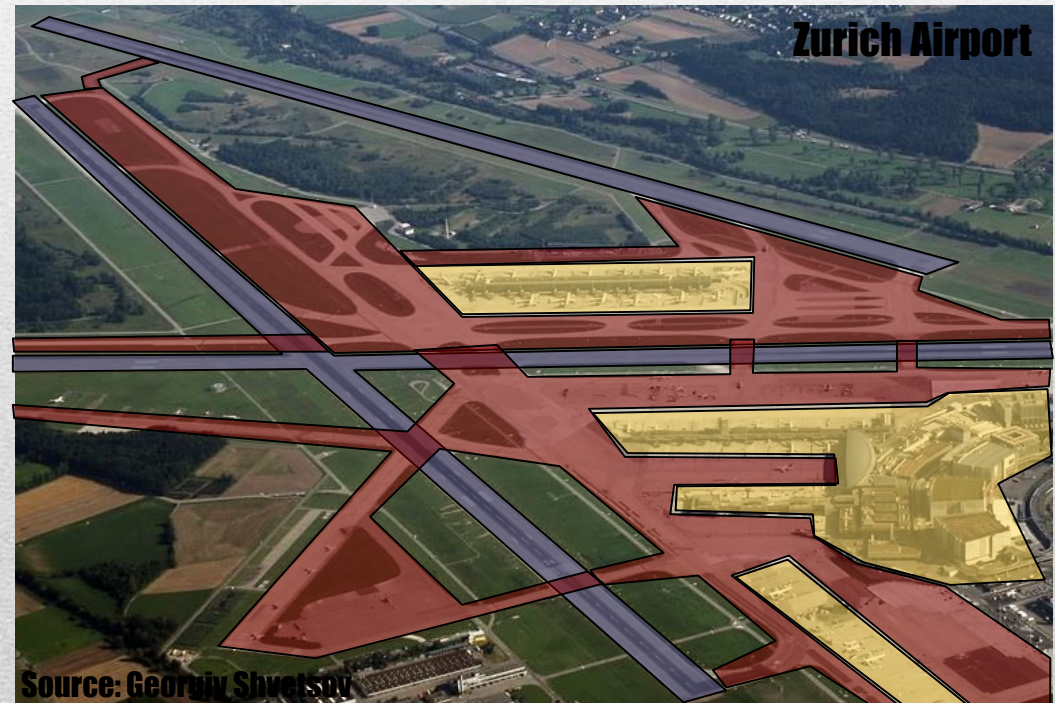




# Airside Airport Operations

## Linked Airport Operations

- With increasing complexity and load at airports, more **advanced decision support systems** are needed
- Airside airport operations are **highly connected**
  - Runway sequencing
    - Departures
    - Arrivals
  - Gate assignment
  - Ground movement





# Taxiing Time Estimation using Fuzzy Rule-based Systems

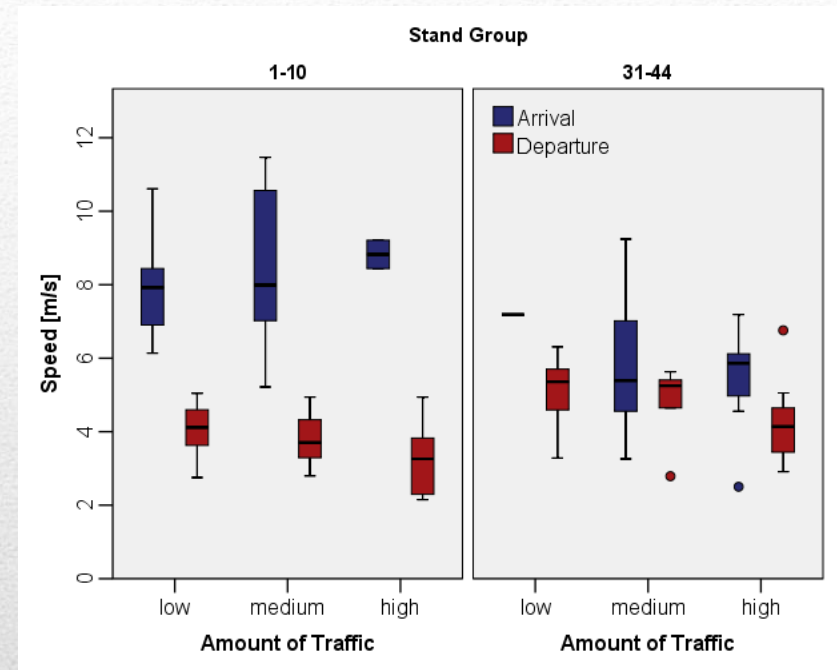


---

**J. Chen**, S. Ravizza, J. Atkin and **P. Stewart** (2011): On the Utilisation of Fuzzy Rule-Based Systems for Taxi Time Estimations at Airports. ATMOS'11, Germany, 09 September, 2011.

## Taxiing Time Estimation using Fuzzy Rule-based Systems-Why Important?

- Major differences in taxi times and speeds
- Required for taxi planning:
  - Taxi times when no other surface traffic is considered
  - fuzzy rule-based systems (Chen *et al.* 2011)



Source: Atkin *et al.*

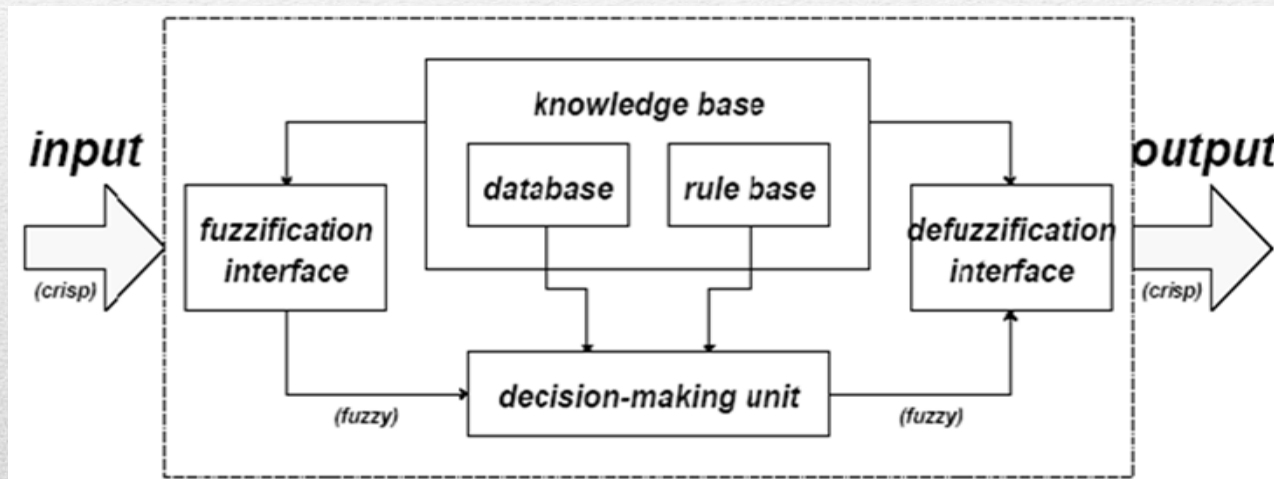
J. Chen, S. Ravizza, J. Atkin and P. Stewart (2011): On the Utilisation of Fuzzy Rule-Based Systems for Taxi Time Estimations at Airports. ATMOS'11, Germany, 09 September, 2011.

- Only accurate taxi time predictions allow realistic comparison with real-world data

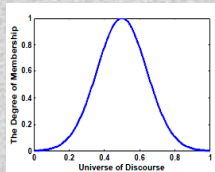


## Taxiing Time Estimation using Fuzzy Rule-based Systems-Why Fuzzy?

- Ability to approximate complex nonlinear systems:
  - FRBS decomposes the system into several sub regions
  - modelling these via different combinations of rules in the rule base
  - the nonlinearity embedded in each membership function



$R_i$  : If  $x_1$  is  $A_i^1$  and  $x_2$  is  $A_i^2, \dots$ , and  $x_j$  is  $A_i^j, \dots$ , and  $x_n$  is  $A_i^n$  Then  $y_i = Z_i$ ,



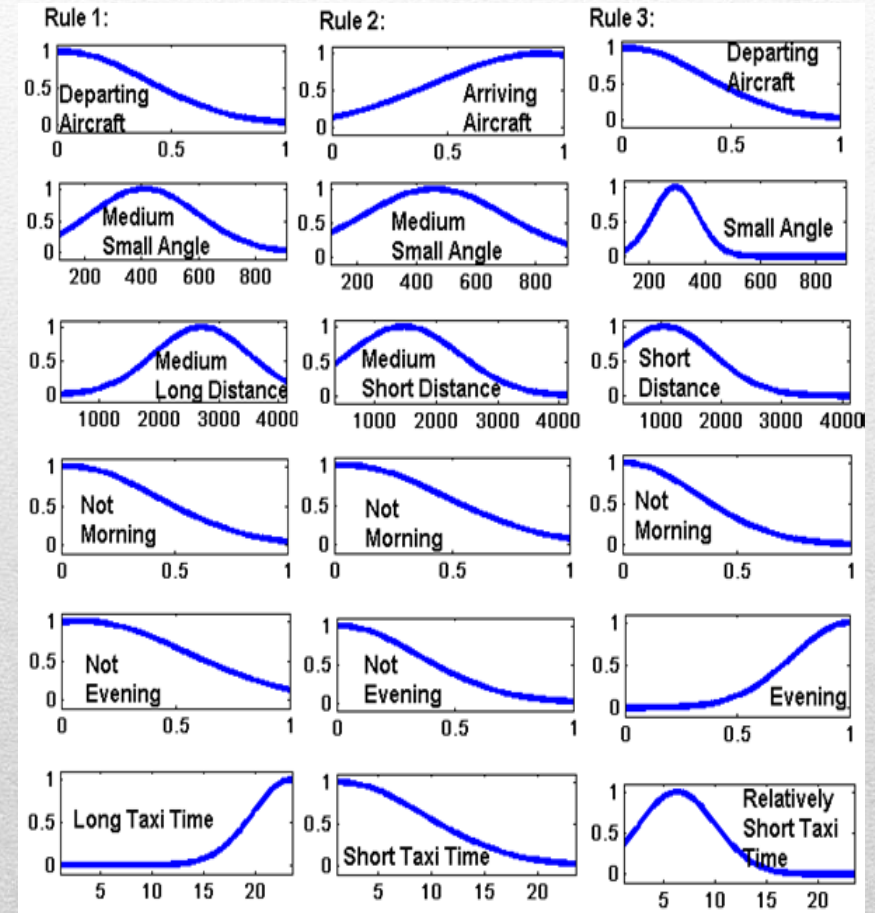
$$\mu_{A_i^j}(x_j) = \exp \left[ -\frac{1}{2} \cdot \frac{(x_j - c_i^j)^2}{(\sigma_i^j)^2} \right]$$

$$\mu_{B_i}(y) = \frac{1}{1 + \left( \frac{y - c_i^y}{\sigma_i^y} \right)^2}$$

## Taxiing Time Estimation using Fuzzy Rule-based Systems-Why Fuzzy?

- Ability to interpret the underlying systems via linguistic terms :

**Rule 1:** If the aircraft is taxiing during the 'day period' and the total turning angle is 'medium small', and the distance is 'medium long', then taxi time is going to take 'long'.



- **LAN** is an important correlation factor with the taxi time;
- Generally **arrivals** tend to taxi quicker than **departing** aircraft, due to the departure queue time.
- **Distance** and **Angle** are also two important correlation factors, with a positive impact on the taxi time.
- **Evening** Mode tends to be more efficient in terms of taxing.



## Taxiing Time Estimation using Fuzzy Rule-based Systems-Why Fuzzy?

- Ability to integrate human expertise due to the rule-base structure and linguistic expression of each rule
- Ability for rules to differ in different regions which makes it easier to understand how the effects of different explanatory variables change according to the values of other explanatory variables

$$y^{crisp} = \frac{\sum_{i=1}^r c_i^y \cdot \mu_i(X) \cdot \int_y \mu_{B_i}(y) dy}{\sum_{i=1}^r \mu_i(X) \cdot \int_y \mu_{B_i}(y) dy}$$

$$\mu_{A_i^j}(x_j) = \exp \left[ -\frac{1}{2} \cdot \frac{(x_j - c_i^j)^2}{(\sigma_i^j)^2} \right]$$

$$\mu_{B_i}(y) = \frac{1}{1 + \left( \frac{y - c_i^y}{\sigma_i^y} \right)^2}$$

### Constrained back-error propagation learning algorithm

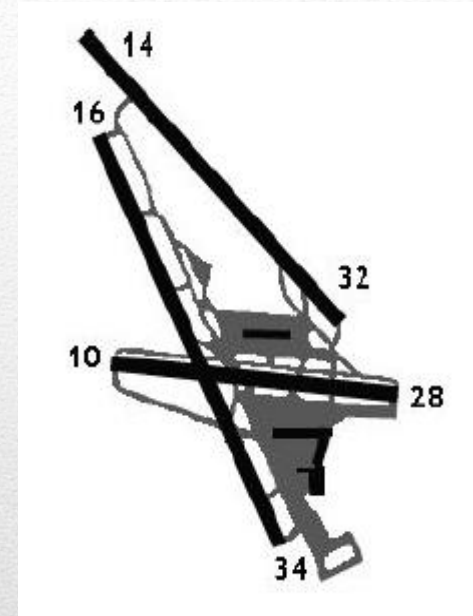


# Taxiing Time Estimation using Fuzzy Rule-based Systems-Problem Description

An entire day's operation for the **19th of October 2007** consisting of **679** movements.

**A rigorous statistical analysis** (Stefan *et al.* in press) suggests:

- Distance
- Log(Distance)
- Log(Angle)
- LAN: 0 for the departing and 1 for the arrival
- Q and N values: indicate the amount of other traffic on the airport surface while the aircraft under consideration is taxiing
- Operational Modes: before 7am, during the day and after 9pm

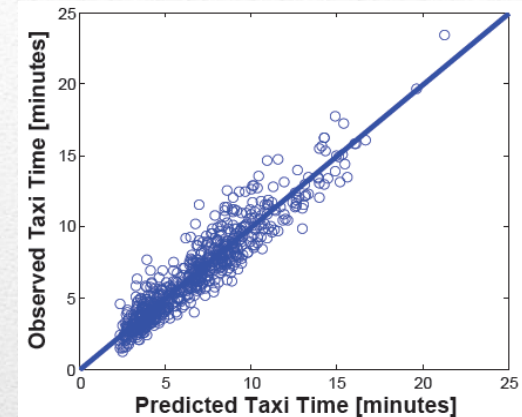


Sketch of airport layout for ZRH

# Taxiing Time Estimation using Fuzzy Rule-based Systems-Results

## Results (1) – Comparison to Linear Regression:

|                   | $\pm 3$ minutes | $\pm 5$ minutes |
|-------------------|-----------------|-----------------|
| Linear regression | 95.6%           | 99.4%           |
| Mamdani FRBS      | 98.8%           | 100%            |



## Results (2) – Validity of Approach without Explicit Transformations:

|                             | $\pm 2$ minutes | $\pm 3$ minutes | $\pm 5$ minutes | $R^2$ |
|-----------------------------|-----------------|-----------------|-----------------|-------|
| With log transformations    | 93.4%           | 98.8%           | 100%            | 0.894 |
| Without log transformations | 92.9%           | 98.7%           | 100%            | 0.890 |

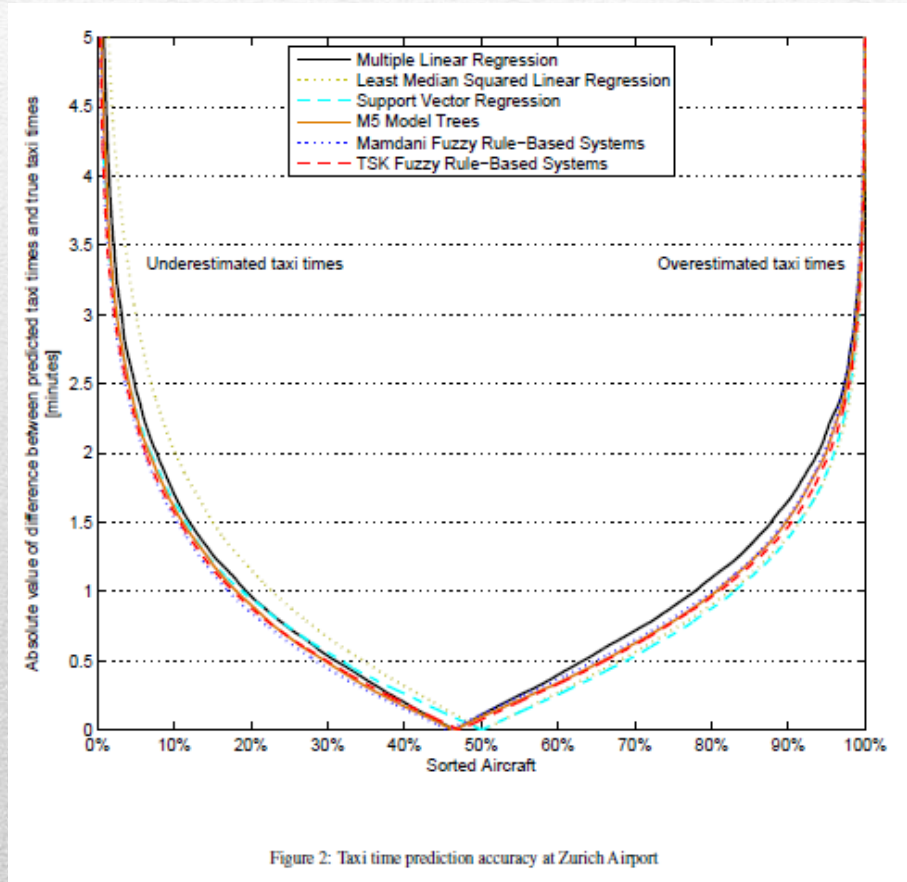
- (1) **Decomposing of the system into sub regions using a set of cooperative rules**
- (2) **An extra degree of freedom to fine-tune a fuzzy model**
- (3) **The hidden transformation functions is learnt, which may not be included within an a priori transformation**



## Taxiing Time Estimation using Fuzzy Rule-based Systems-Comparison

Comparisons among different regression approaches:

- Historic data from two major European airports
- 15 repetitions and 10-fold cross-validation



## Taxiing Time Estimation using Fuzzy Rule-based Systems-Comparison

$$R_1 : \text{If } x_1 \text{ is } A_1^1 \text{ and } x_2 \text{ is } A_1^2, \dots, \text{ and } x_j \text{ is } A_1^j \text{ Then } y_1 = b_1^0 + b_1^1 \cdot x_1 + \dots + b_1^j \cdot x_j$$

$$\dots$$

$$R_k : \text{If } x_1 \text{ is } A_k^1 \text{ and } x_2 \text{ is } A_k^2, \dots, \text{ and } x_j \text{ is } A_k^j \text{ Then } y_k = b_k^0 + b_k^1 \cdot x_1 + \dots + b_k^j \cdot x_j.$$

Table 2: Comparisons of performance measures for Stockholm-Arlanda Airport and Zurich Airport

| Performance Measure         | Airport | LinReg | LMS    | SMOreg        | M5P    | Mamdani | TSK           |
|-----------------------------|---------|--------|--------|---------------|--------|---------|---------------|
| Root mean-squared error     | ARN     | 1.52   | 1.57   | 1.50          | 1.51   | 1.46    | <b>1.44</b>   |
|                             | ZRH     | 1.47   | 1.60   | 1.32          | 1.36   | 1.33    | <b>1.30</b>   |
| Mean-absolute error         | ARN     | 1.14   | 1.14   | 1.09          | 1.13   | 1.07    | <b>1.06</b>   |
|                             | ZRH     | 1.08   | 1.10   | <b>0.96</b>   | 0.99   | 0.97    | <b>0.96</b>   |
| Root relative-squared error | ARN     | 45.70% | 47.47% | 45.27%        | 45.54% | 44.19%  | <b>43.53%</b> |
|                             | ZRH     | 29.29% | 31.76% | 26.28%        | 27.00% | 26.41%  | <b>25.89%</b> |
| Relative-absolute error     | ARN     | 45.80% | 45.92% | 43.98%        | 45.61% | 43.28%  | <b>42.83%</b> |
|                             | ZRH     | 26.85% | 27.52% | <b>23.87%</b> | 24.55% | 24.30%  | 23.93%        |

Table 3: Comparisons of accuracies for Stockholm-Arlanda Airport and Zurich Airport

| Accuracy                     | Airport | LinReg        | LMS           | SMOreg        | M5P           | Mamdani       | TSK           |
|------------------------------|---------|---------------|---------------|---------------|---------------|---------------|---------------|
| Accuracy within $\pm 1$ min  | ARN     | 54.28%        | 56.02%        | 57.86%        | 54.61%        | 58.21%        | <b>58.80%</b> |
|                              | ZRH     | 58.38%        | 59.66%        | <b>64.05%</b> | 62.49%        | 62.97%        | 63.33%        |
| Accuracy within $\pm 2$ min  | ARN     | 85.30%        | 85.18%        | 84.91%        | 85.19%        | 86.73%        | <b>86.81%</b> |
|                              | ZRH     | 86.12%        | 85.99%        | 88.98%        | 88.15%        | 88.55%        | <b>89.07%</b> |
| Accuracy within $\pm 3$ min  | ARN     | 95.40%        | 94.80%        | 94.32%        | 95.43%        | 95.72%        | <b>96.16%</b> |
|                              | ZRH     | 95.55%        | 94.26%        | 96.60%        | 96.46%        | 96.54%        | <b>96.89%</b> |
| Accuracy within $\pm 5$ min  | ARN     | 99.16%        | 98.81%        | 99.16%        | <b>99.18%</b> | 98.97%        | 99.08%        |
|                              | ZRH     | 99.21%        | 98.56%        | 99.45%        | 99.46%        | 99.53%        | <b>99.62%</b> |
| Accuracy within $\pm 10$ min | ARN     | <b>99.92%</b> | <b>99.92%</b> | <b>99.92%</b> | <b>99.92%</b> | <b>99.92%</b> | <b>99.92%</b> |
|                              | ZRH     | 99.92%        | 99.87%        | 99.97%        | 99.97%        | <b>99.98%</b> | 99.97%        |

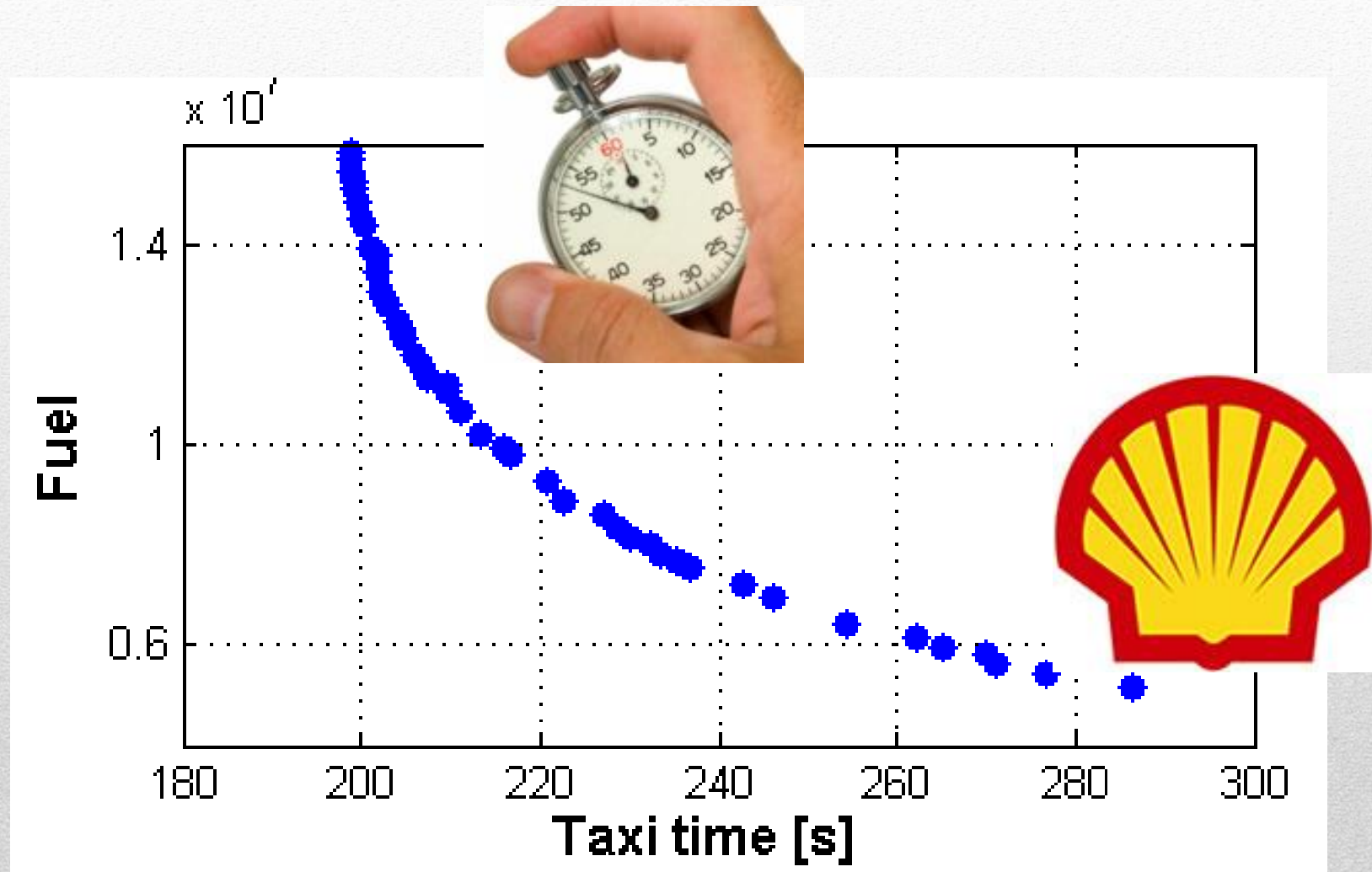


## Taxiing Time Estimation using Fuzzy Rule-based Systems-Conclusions

Taxiing time estimation can be used for **ground movement optimiser**

- Algorithms need taxi time predictions for isolated aircraft.
- The effects of the amount of traffic can be eliminated by setting all the corresponding variables to 0.
- Unlike multiple linear regression, Mamdani and Sugeno FRBS presents certain corporation among different rules which is believed to be able to deal with the transition behaviour between different sub regions.
- Fuzzy rule-based systems are not used quite often and deserve more exploration in this field for other airport, such as **Manchester International Airport**.

## Trade-off between Time and Fuel using Multi-Objective Optimisation



**J. Chen** and **P. Stewart** (2011): Planning Aircraft Taxiing Trajectories via a Multi-Objective Immune Optimisation ICNC'11-FSKD'11, Shanghai, China, 26-28 July, 2011.

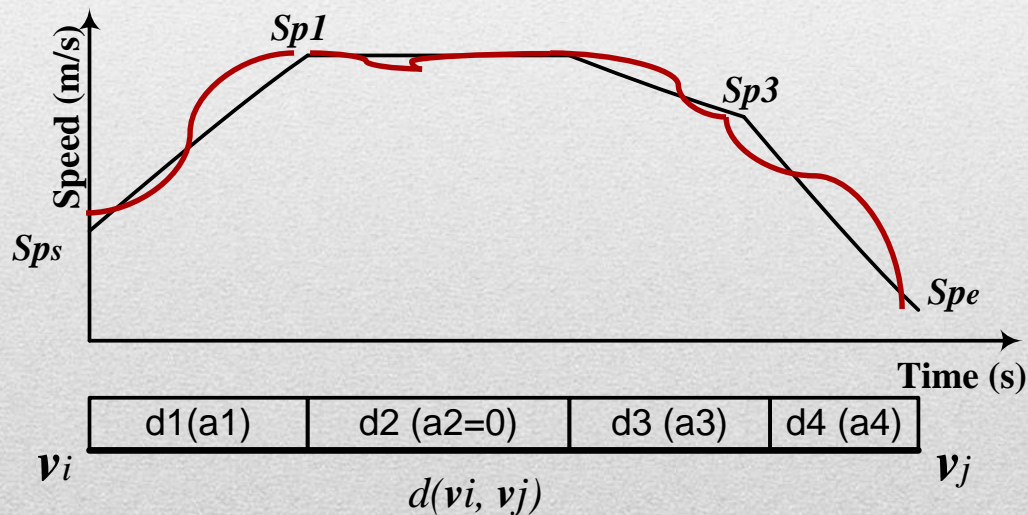


# Trade-off between Time and Fuel using Multi-Objective Optimisation

## Assumptions:

Less taxi time  Less fuel consumption and pollutant

## Trajectories Planning for a single unimpeded aircraft

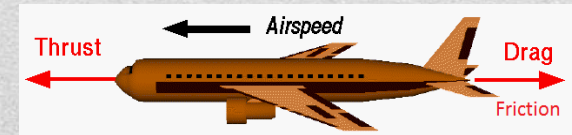


NB:  $a2=0$ ;  $a3=f(d3,d4,a4,Sp1)$ ;  $a4=0.1g$ ;  $d3=d(v_i, v_j)-d1-d2-d4$

## Aircraft Model:

Mass point model: mass, friction, thrust

Newton's basic mechanics



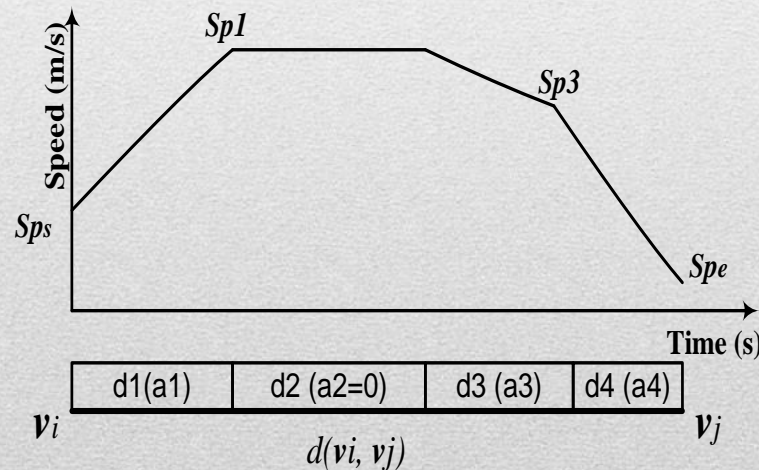
# Trade-off between Time and Fuel using Multi-Objective Optimisation: PAIA

## Objectives:

- 1<sup>st</sup> Objective: Total Taxiing Time  $T$
- 2<sup>nd</sup> Objective: Fuel Consumption Index

$$\int_0^T [TR(t) \cdot (1 + a(t))] \cdot dt$$

## Decision Variables and Constraints:



NB:  $a2=0$ ;  $a3=f(d3,d4,a4,Sp1)$ ;  $a4=0.1g$ ;  $d3=d(v_i, v_j)-d1-d2-d4$

**{a1, d1, d2, d4}**

(1)  $a$ :  $a(t) \leq a_{max}$ .

(2)  $a1$ :  $a_{1-l} = \frac{Sp_e^2 - Sp_s^2}{2 \cdot d(v_i, v_j)}$ .

(3)  $d1$ :  $d_{1-l} = \frac{Sp_e^2 - Sp_s^2}{2 \cdot a_1}$ .

(4)  $d2$ :  $d_{2-u} = d(v_i, v_j) - d_1 - \frac{Sp_1^2 - Sp_e^2}{2 \cdot a_{max}}$ .

(4)  $d2$ :  $d_{2-l} = d(v_i, v_j) - d_1 - \frac{Sp_1^2 - Sp_e^2}{2 \cdot a_{min-d}}$ .

(5)  $d4$ :  $d_{4-u} = \frac{Sp_1^2 - Sp_e^2}{2 \cdot a_{max}}$ .

$d_{4-l} = 0$



# Trade-off between Time and Fuel using Multi-Objective Optimisation: Data Sets

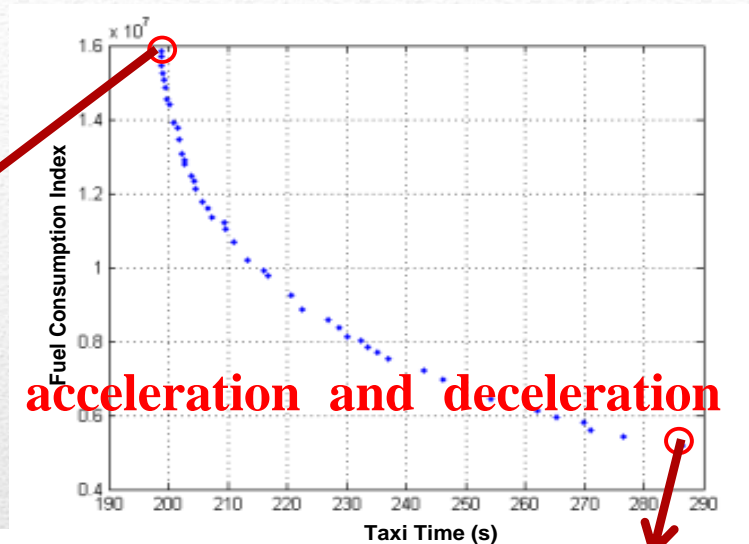


## Needed Information about Aircraft Taxiing:

- (i) The length of each Arc;
- (ii) The taxi speed at the start of each Arc;
- (iii) The taxi speed at the end of each Arc;
- (iv) The maximum taxi speed for each Arc;

| Edge No. | Information                  |        |        |       |
|----------|------------------------------|--------|--------|-------|
|          | Edge Description             | (knot) | (knot) | (m)   |
| 1        | Straight T.W. <sup>a</sup>   | 0      | 10     | 153.8 |
| 2        | Turning T.W.                 | 10     | 10     | 61.5  |
| 3        | Straight T.W.                | 10     | 10     | 92.3  |
| 4        | Turning T.W.                 | 10     | 10     | 61.5  |
| 5        | Straight T.W.                | 10     | 10     | 246.2 |
| 6        | Turning T.W.                 | 10     | 10     | 153.8 |
| 7        | Straight T.W.W. <sup>b</sup> | 10     | 0      | 215.4 |
| 8        | Straight T.W.                | 0      | 10     | 138.5 |
| 9        | Turning T.W.                 | 10     | 10     | 92.3  |
| 10       | Runway Acc. H. <sup>c</sup>  | 10     | 0      | 230.8 |

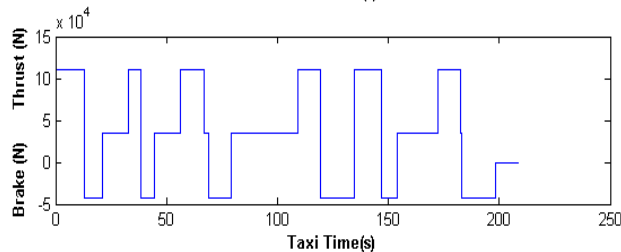
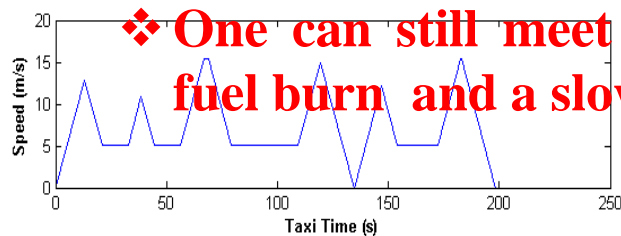
# Trade-off between Time and Fuel using Multi-Objective Optimisation: Results



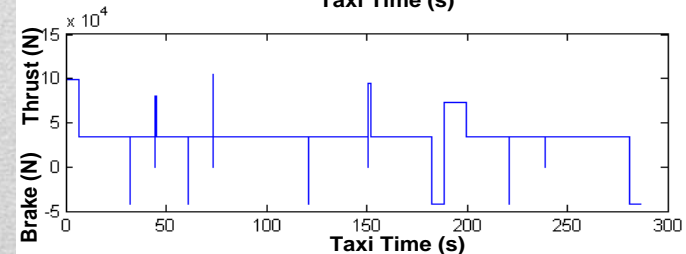
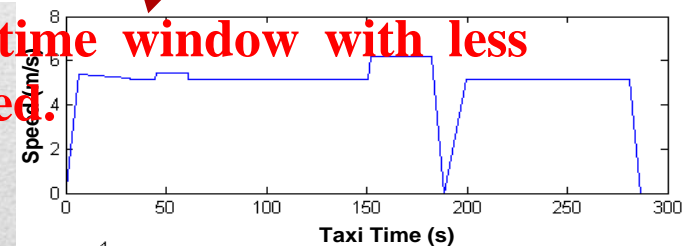
Fast taxi speed  
Higher fuel consumption

❖ Excessive acceleration and deceleration may not be favoured

Slow taxi speed  
Lower fuel consumption



❖ One can still meet the target time window with less fuel burn and a slower taxi speed.

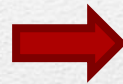




## Trade-off between Time and Fuel using Multi-Objective Optimisation: **Insights**

- ❖ The actual modelling of fuel burn objective function plays an important role:

$$\int_0^T [TR(t) \cdot (1 + a(t))] \cdot dt$$



- Using Base of Aircraft Data (BADA)
- A More Realistic Aircraft Model: Physical models, throttle to thrust to fuel burn data, brake to thrust data, etc.

- ❖ The information of the following is really important :

- (i) The taxi speed at the start of each Arc;
- (ii) The taxi speed at the end of each Arc;
- (iii) The maximum taxi speed for each Arc;



## Combined Trade-off and Routing and Scheduling Algorithm



### Interactions between multiple aircraft

---

S. Ravizza, **J. Chen**, J. A. D. Atkin, E. K. Burke and **P. Stewart** (2013): The Trade-off Between Taxi Time and Fuel consumption in Airport Ground Movement. Journal of Public Transportation. DOI 10.1007/s12469-013-0060-1.



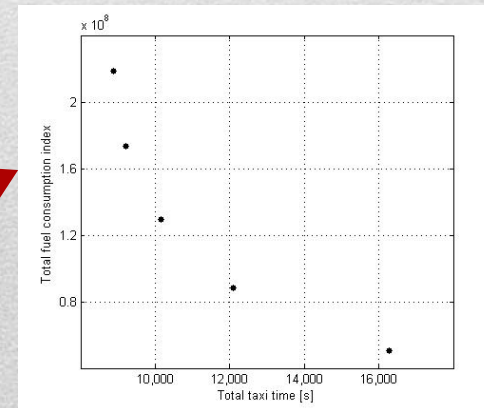
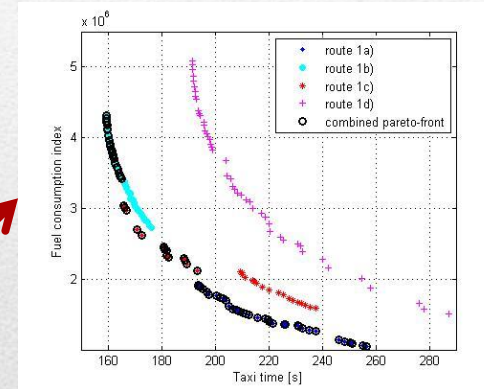
# Combined Trade-off and Routing and Scheduling Algorithm: Integration

**Novel concept** using combined:

**k-QPPTW**: Finds best possible routes for an aircraft

**PAIA**: Finds Pareto-front for different speed profiles for each of these routes

- 1 Sort all flights by pushback/landing time
- 2 **foreach** objective function discretisation  $i \leftarrow 1$  to  $l$  **do**
- 3   **foreach** aircraft  $a$  **do**
- 4     Find best  $k$  routes w.r.t. minimal taxi times using  $k$ -QPPTW algorithm
- 5     **foreach** route  $k$  of aircraft  $a$  **do**
- 6       Approximate pareto-front of both objectives, using population adaptive immune algorithm (PATT-PAIA)
- 7     Generate combined pareto-front for source-destination pair of aircraft  $a$
- 8     Discretise this pareto-front into  $l$  roughly equally spaced points
- 9     Select the  $i$ th point and reserve the relevant route for aircraft  $a$
- 10   Save the accumulated values for all aircraft for both objective functions for the global pareto-front
- 11 **Output**: Global discretised pareto-front



## Combined Trade-off and Routing and Scheduling Algorithm: Results

- One week's operation at Zurich Airport
- 2<sup>nd</sup> objective function:  $F_{Total} = F_{Resistance} + F_{Acceleration}$

|                                  | Mon  | Tue  | Wed  | Thu  | Fri  | Sat  | Sun  |
|----------------------------------|------|------|------|------|------|------|------|
| <b>Ø Taxi time</b>               |      |      |      |      |      |      |      |
| Time-efficient [s]               | 156  | 157  | 128  | 174  | 152  | 165  | 154  |
| Fuel-efficient [s]               | 285  | 293  | 214  | 320  | 292  | 316  | 295  |
| Growth                           | 83%  | 87%  | 67%  | 84%  | 92%  | 91%  | 91%  |
| <b>Ø Fuel cons. index</b>        |      |      |      |      |      |      |      |
| Time-efficient [ $\times 10^3$ ] | 3832 | 3291 | 3492 | 4002 | 3173 | 3754 | 3718 |
| Fuel-efficient [ $\times 10^3$ ] | 884  | 762  | 742  | 922  | 700  | 849  | 823  |
| Growth                           | 334% | 332% | 371% | 334% | 353% | 342% | 352% |
| Number of aircraft               | 57   | 58   | 46   | 58   | 56   | 63   | 52   |



## Combined Trade-off and Routing and Scheduling Algorithm: Results

- 2 different fuel burn types:
  - Acceleration (10% of maximal fuel flow)
  - Taxiing with constant speed, deceleration, holding (5.5%)

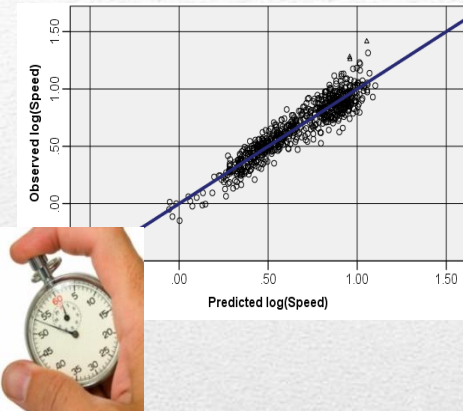
|                     | Different objective function |
|---------------------|------------------------------|
| <b>Ø Taxi time</b>  |                              |
| Time-efficient [s]  | 155.5                        |
| Fuel-efficient [s]  | 156.7                        |
| Growth              | 0.8%                         |
| <b>Ø Fuel flow</b>  |                              |
| Time-efficient [kg] | 23.8                         |
| Fuel-efficient [kg] | 23.5                         |
| Growth              | 1.2%                         |

## Combined Trade-off and Routing and Scheduling Algorithm: Conclusions

- Depends very much upon the actual modelling of the fuel-based objective function (physics-based vs. fuel flow).
  - If the more realistic modelling of the fuel-based objective function suggests that we can gain significant improvement in terms of fuel consumption using the optimised speed profiles, this information should also feedback to pilots so that they will follow such speed profiles.
  - These appear not to be well understood and deserve more investigation on different airport.
-



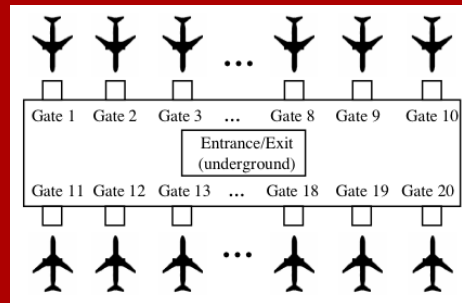
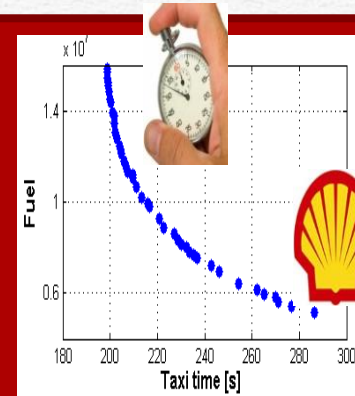
## Future Work



More accurate  
prediction

**Multi-domain  
Modelling  
System identification**

| Taxiway<br>Arc No. | Start<br>Speed | End<br>Speed | Maximum<br>Speed | Taxi<br>Time | Fuel<br>consumption |
|--------------------|----------------|--------------|------------------|--------------|---------------------|
| No. 1              |                |              |                  |              |                     |
| No. 2              |                |              |                  |              |                     |
| No. n              |                |              |                  |              |                     |



Integration

➤ Semi automated  
taxiing

➤ Fully automated  
taxiing

Novel concepts

**Thanks!!**

---